

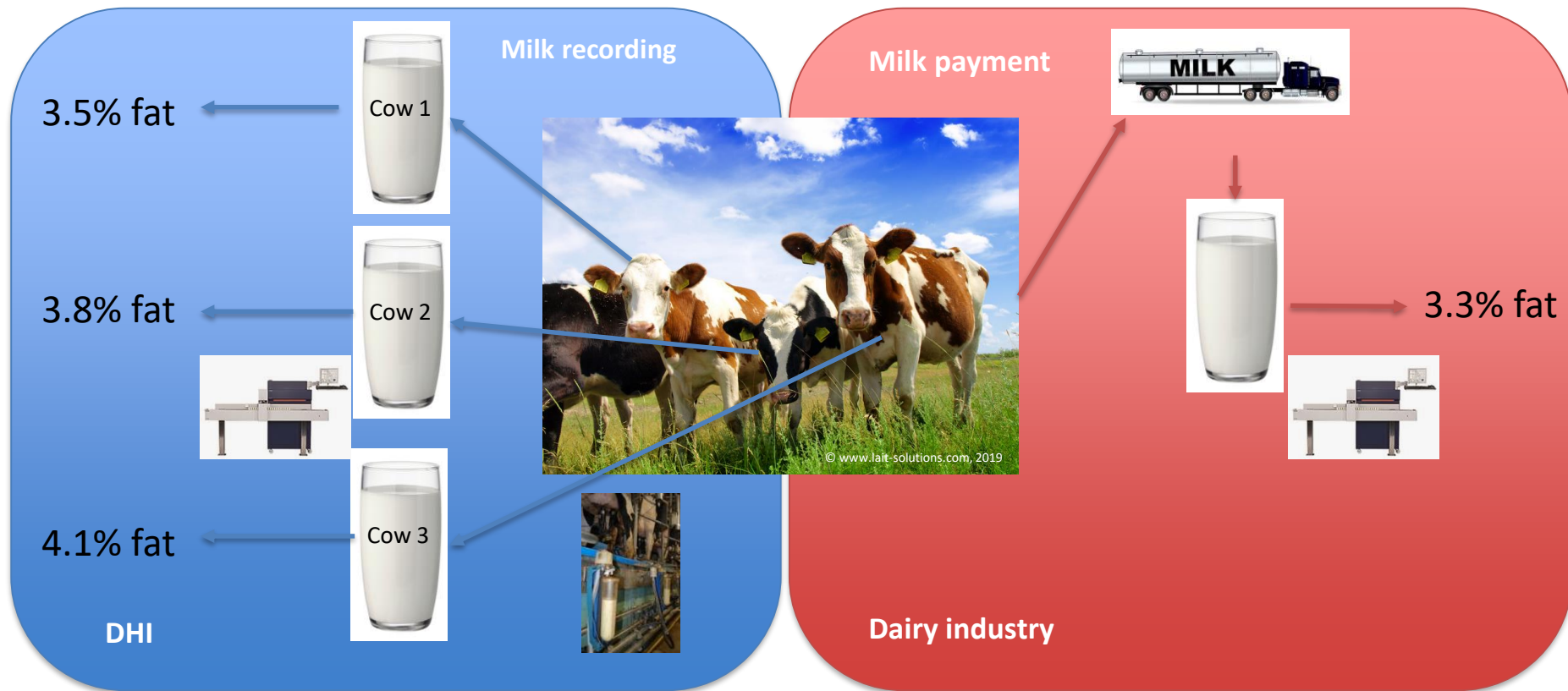
Lei ZHANG

Ma Y.; DEHARENG F.; Grelet C.; COLINET F.; GENGLER N.; SOYEURT H.

**Can the calculation of a spectral Global H distance  
ensure the quality of international based MIR predictions?**



# Milk Recording Scheme



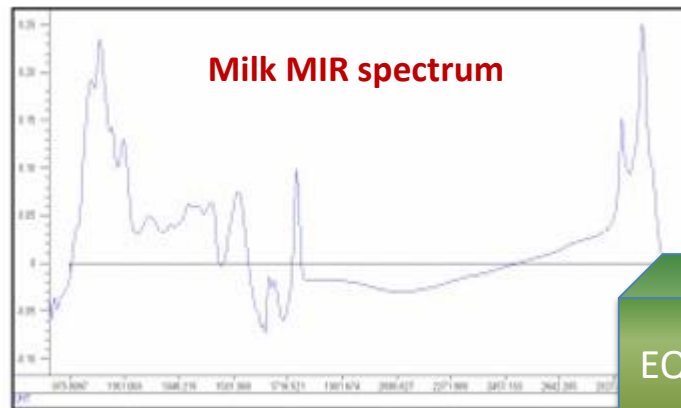
# Milk Analysis



Milk recording  
(About 1 month for each  
cow)



%fat

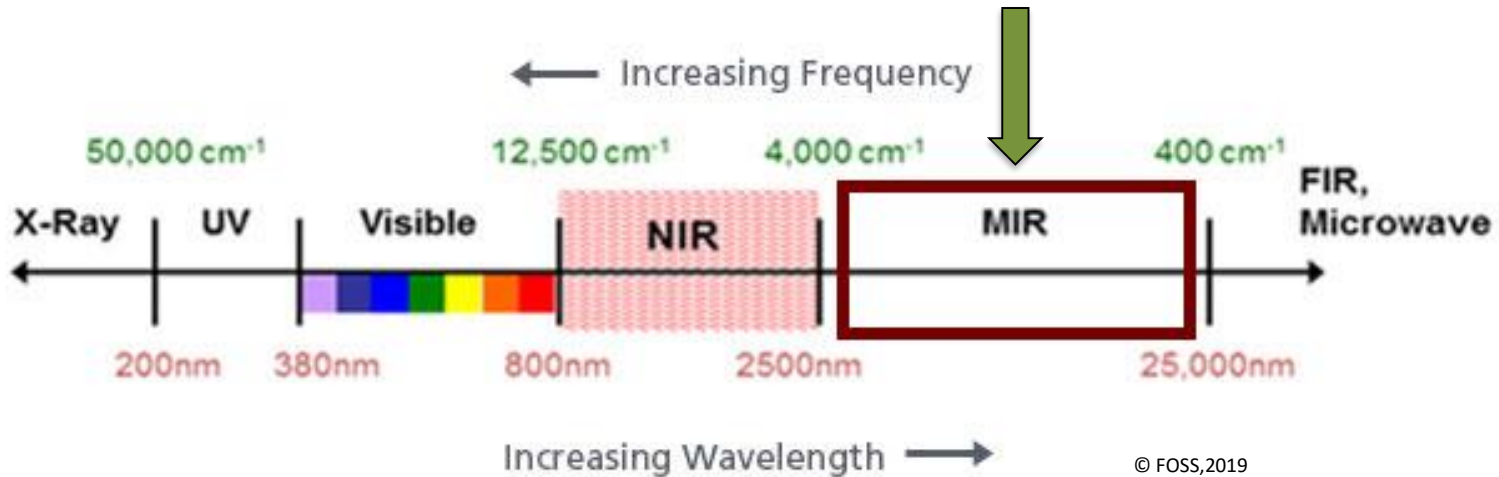


EQUATION



# What is Mid-infrared spectrum?

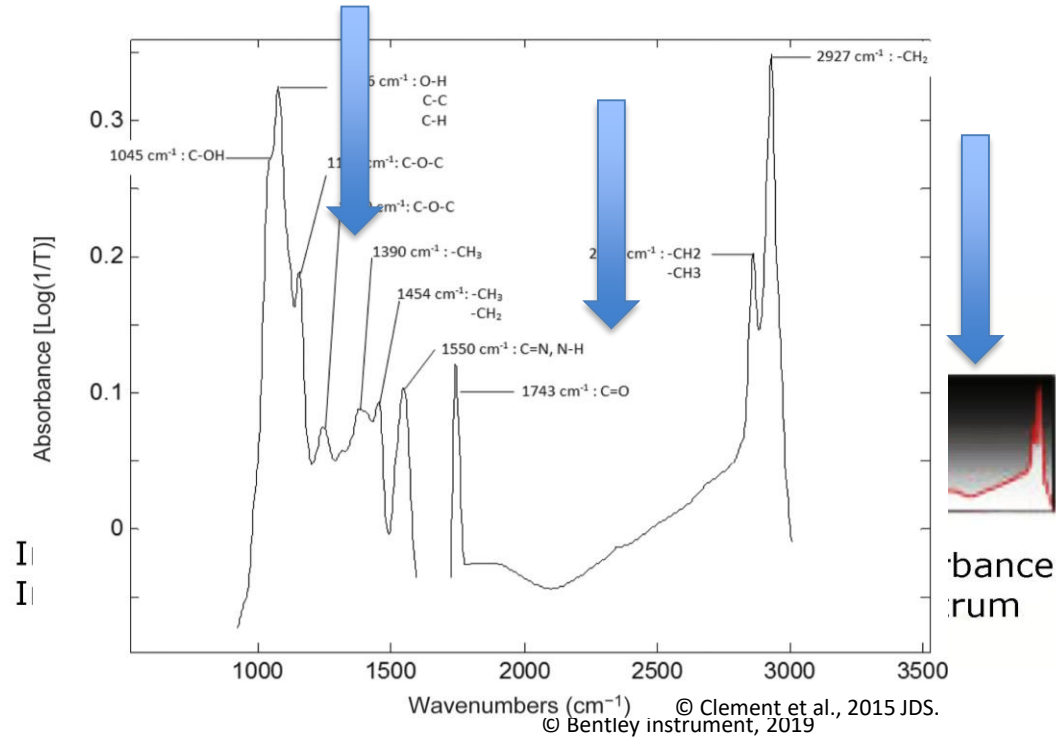
- Approximately 2,500-25,000nm (4,000-400  $\text{cm}^{-1}$ )



Frequency = 1 / wavelength

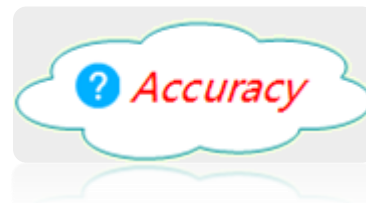
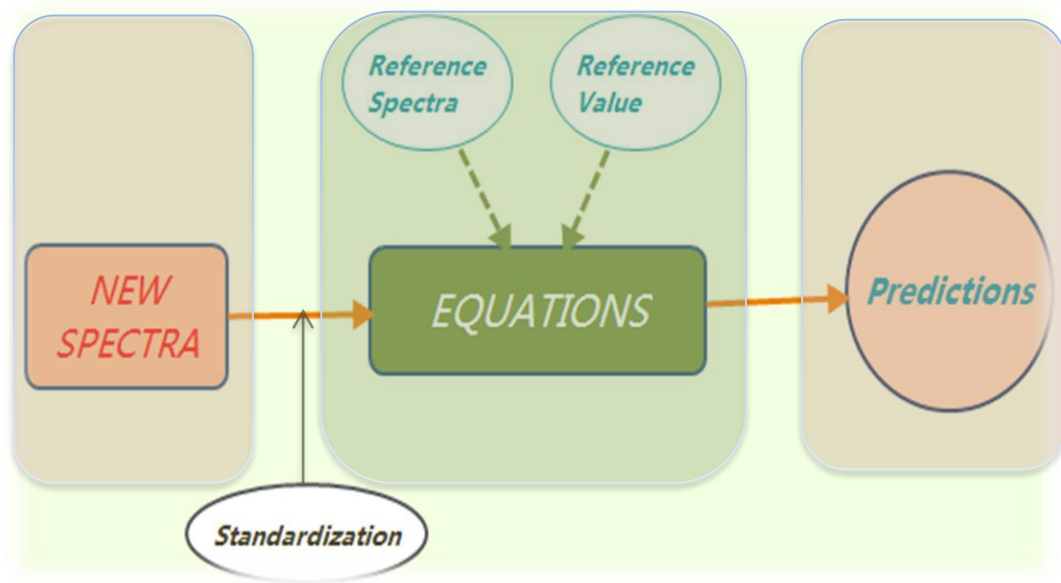


# Principle of MIR spectrometry





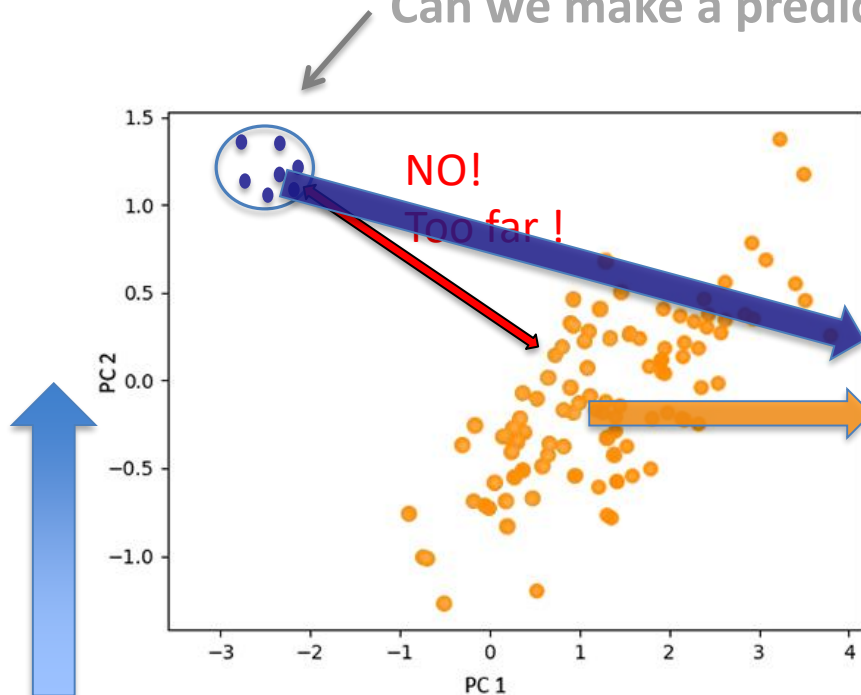
# How can we make a prediction ?



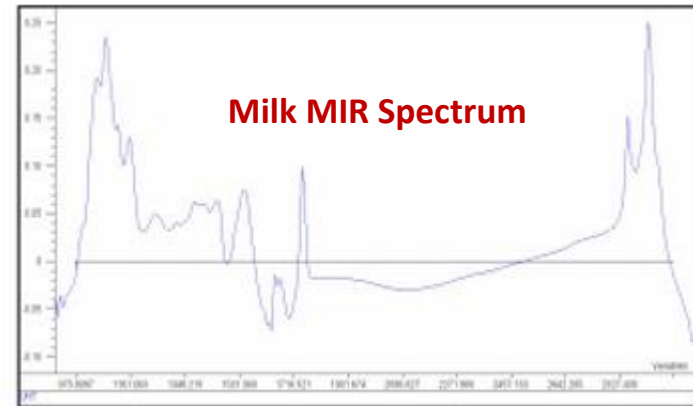


# Can we make a prediction for all spectra ?

Can we make a prediction from those spectra?



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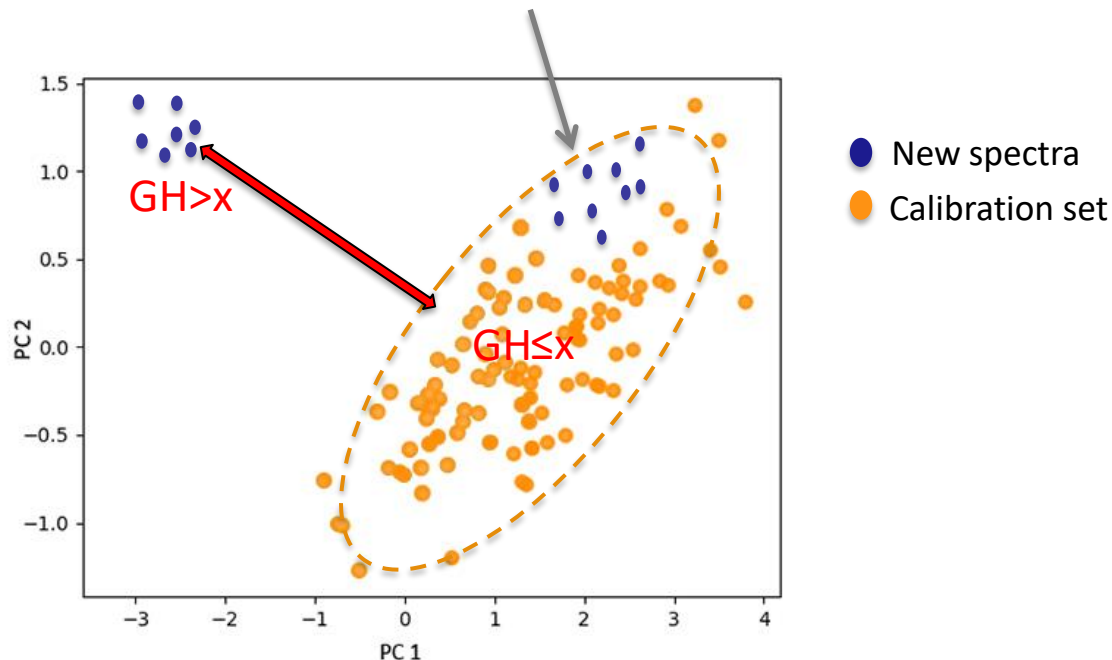






# Can we make a prediction for all spectra ?

Can I make a prediction from those spectra?



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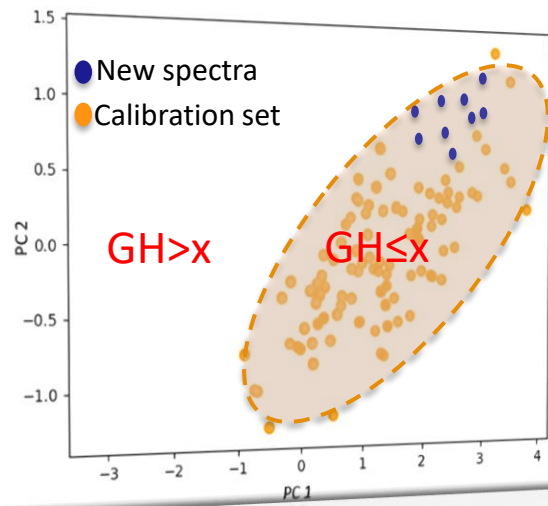


© Wikipedia  
P.C. Mahalanobis  
(1893 – 1972)

## Mahalanobis Distance:

$$D_M(\vec{x}) = \sqrt{(\vec{x} - \vec{\mu})^T S^{-1} (\vec{x} - \vec{\mu})}$$

Where:  $\vec{x}$  is PC scores of one spectrum;  
 $\vec{\mu}$  is the mean of PC scores of spectra in  
the calibration set;  
 $S$  is covariance matrix between PC scores  
of the calibration spectra



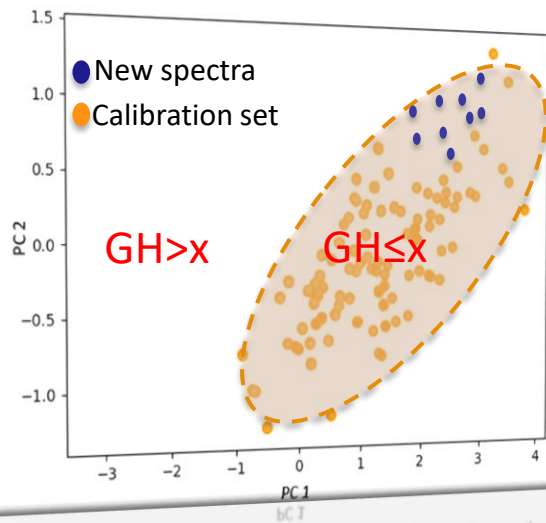
$$GH = \frac{DM}{nPCs}$$

## Mahalanobis Distance:

$$D_M(\vec{x}) = \sqrt{(\vec{x} - \vec{\mu})^T S^{-1} (\vec{x} - \vec{\mu})}$$

**GH:** Global H which is the  
Standardized Mahalanobis  
Distance

$$GH = \frac{DM}{nPCs}$$



Where:  
**DM** is the distance calculated  
from the formula;  
**nPCs** is the number of the  
principal components from PCA

# What is the accuracy of prediction of international spectrum?

Milk  
Recording

MIR

STD

MIR<sub>STD</sub>

MIR<sub>Cal</sub>

## Standardization of milk mid-infrared spectra from a European dairy network

[C. Grelet](#)<sup>1</sup>, [J.A. Fernández Pierna](#)<sup>1</sup>, [P. Dardenne](#), [V. Baeten](#), [F. Dehareng](#)<sup>2</sup>  

Walloon Agricultural Research Center, Valorisation of Agricultural Products Department, 24 Chaussée de Namur, 5030 Gembloux, Belgium

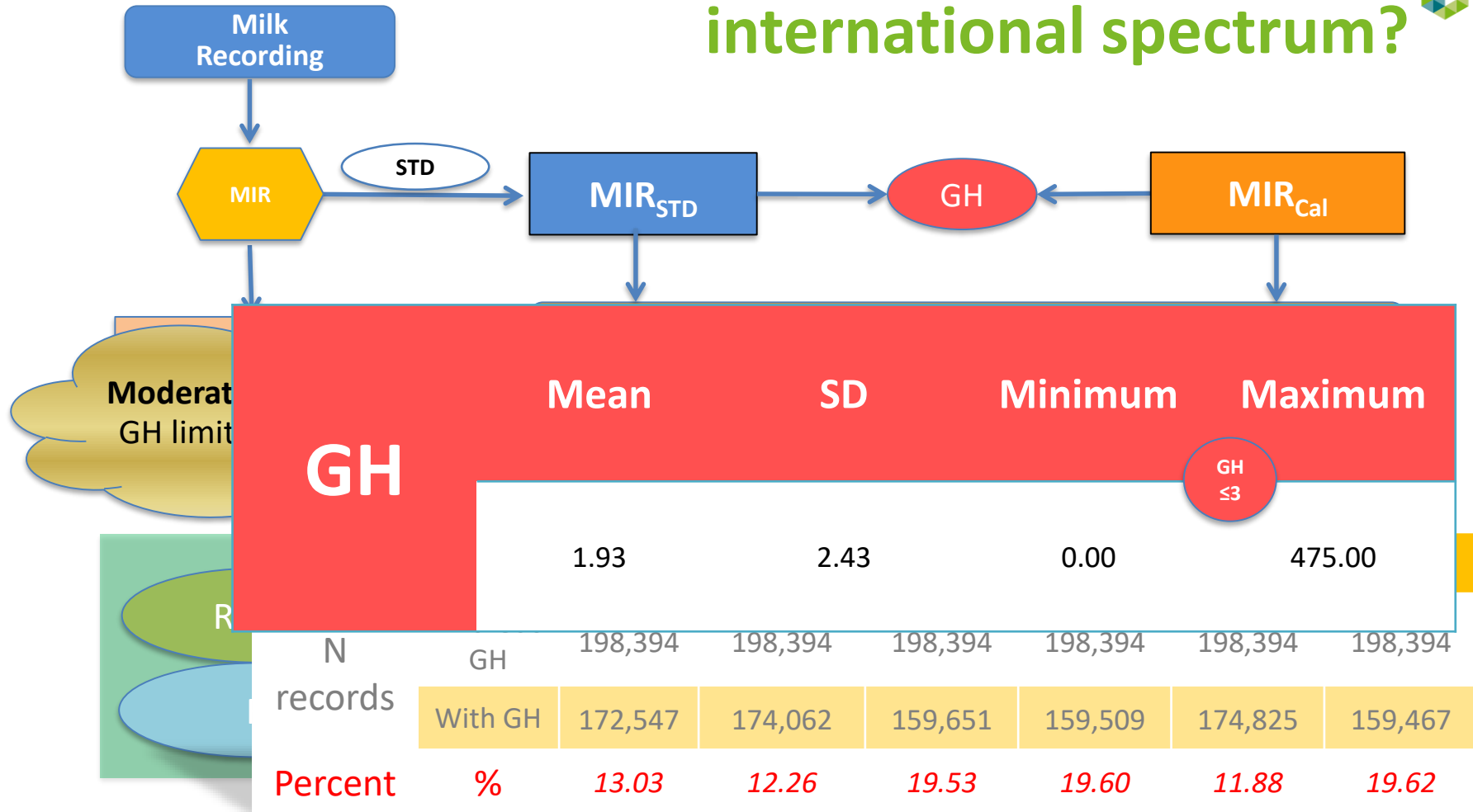
Open Archive  PlumX Metrics

DOI: <https://doi.org/10.3168/jds.2014-8764>

R

Prediction


# What is the accuracy of prediction of international spectrum?





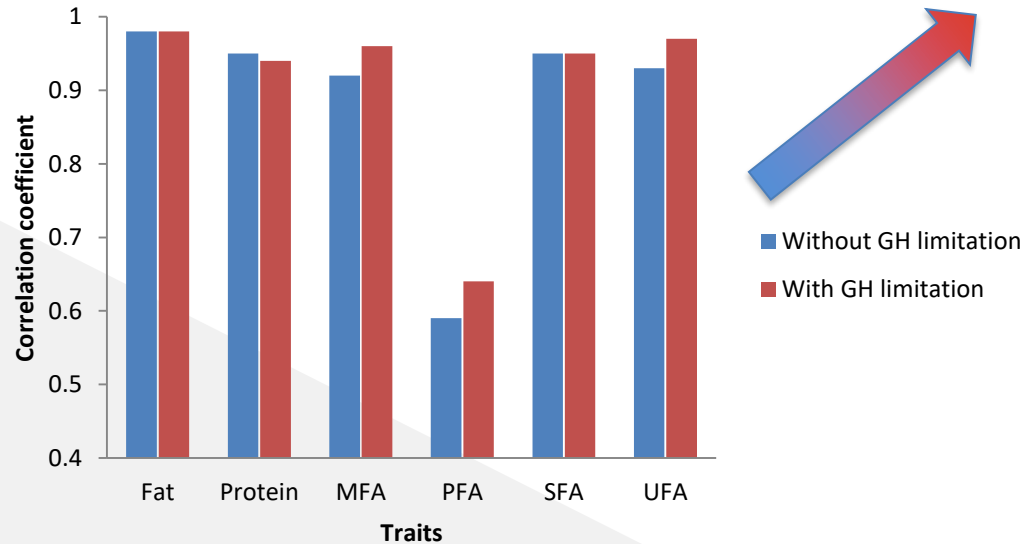
# Descriptive statistics

Table 1. Descriptive statistics of predicted value

Traits g/dL	Reference value		Predicted value		Predicted value (GH ≤ 3)	
	Mean	SD	Mean	SD	Mean	SD
Fat	3.97	0.95	3.99	0.95	3.90	0.86
Protein	3.43	0.40	3.53	0.46	3.52	0.39
MFA	0.86	0.27	1.15	0.36		0.31
PFA	0.07	0.04	0.15	0.05		0.04
SFA	2.62	0.67	2.64	0.68	2.59	0.62
UFA	0.93	0.31	1.29	0.39	1.25	0.34

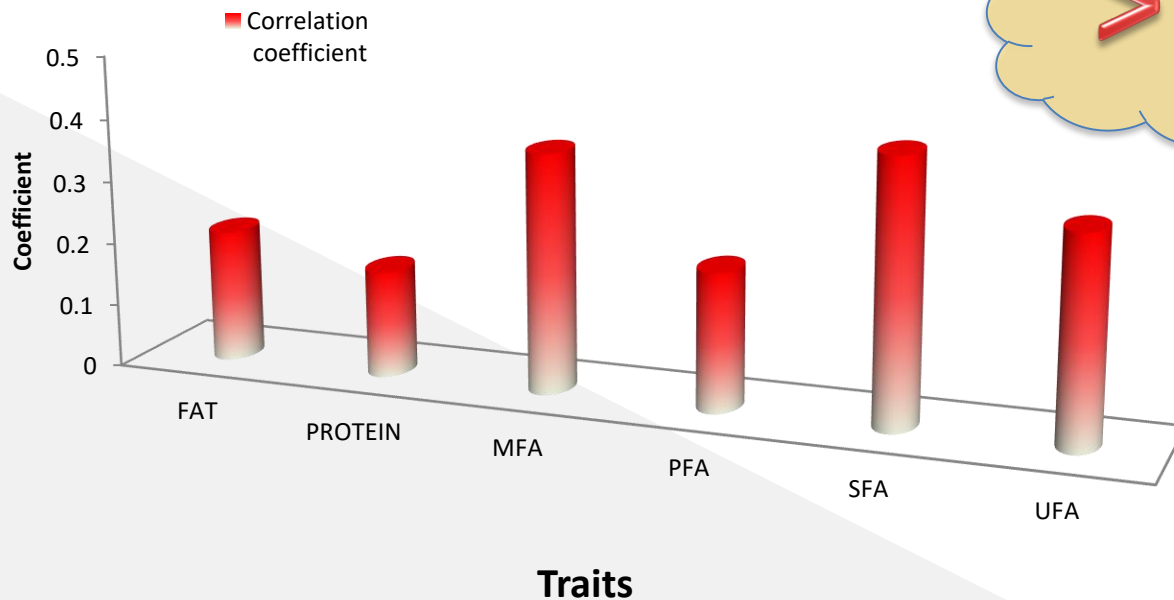
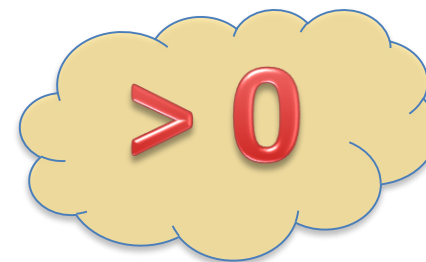


# The correlation coefficient



Why?

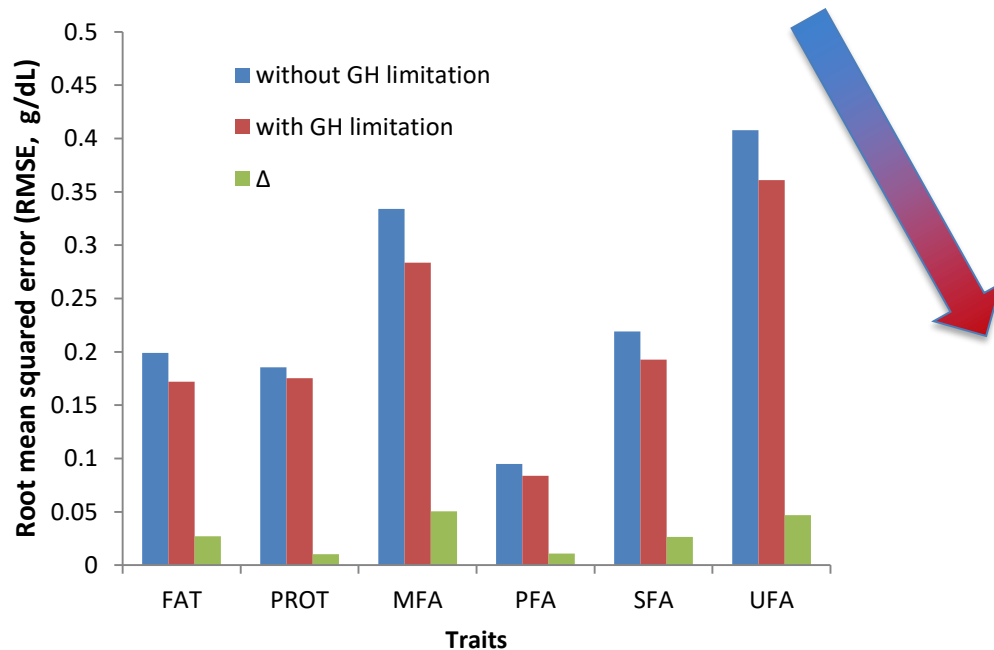
# Squared residual and GH







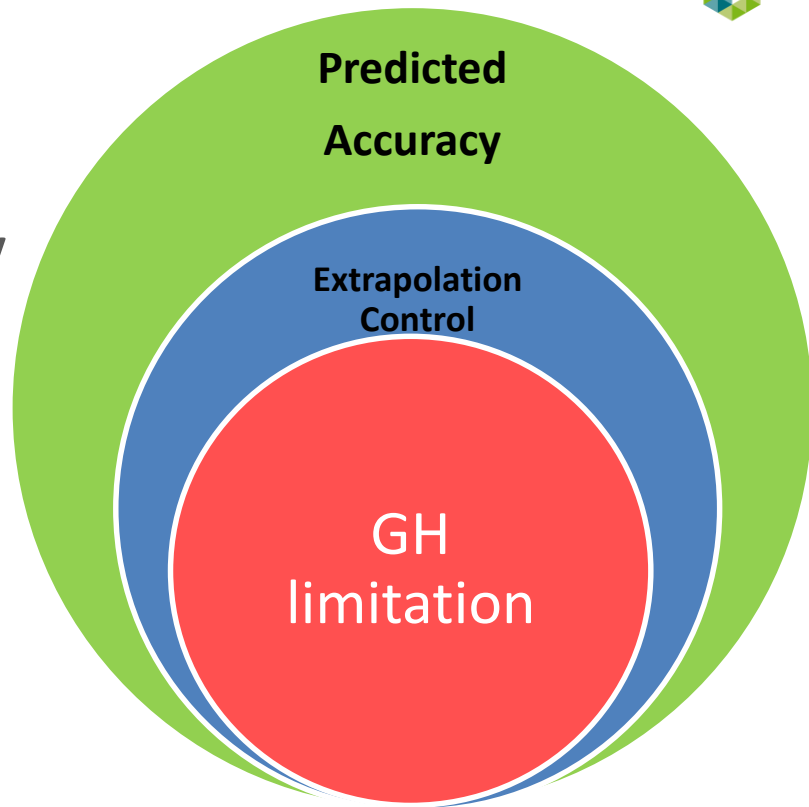
# GH limitation decreased RMSE for most traits





# Conclusion:

- ▶ GH limitation helps to **ensure the quality** of the MIR predictions
- ▶ It allows **avoiding spectral extrapolation**
- ▶ More work needed to be done to get **more accurate** predictions...



Thanks for your attention!

Email: [lei.zhang@doct.uliege.be](mailto:lei.zhang@doct.uliege.be)





Ma Y.; DEHARENG F.; Grelet C.; COLINET F.; GENGLER N.; SOYEURT H., &  
Lei ZHANG

Email: [lei.zhang@doct.uliege.be](mailto:lei.zhang@doct.uliege.be)

# Additional information:

## Why do PCA?

- ▶ To decrease the dimensionality of the raw data
- ▶ To make it easy for calculating the inverse of the covariance matrix

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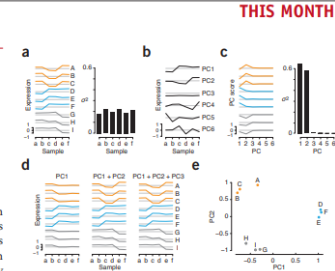
### POINTS OF SIGNIFICANCE

#### Principal component analysis

PCA helps you interpret your data, but it will not always find the important patterns.

Principal component analysis (PCA) simplifies the complexity in high-dimensional data while retaining trends and patterns. It does this by transforming the data into fewer dimensions, which act as summaries of features. High-dimensional data are very common in biology and arise when multiple features, such as expression of many genes, are measured for each sample. This type of data presents several challenges that PCA mitigates: computational expense and an increased error rate due to multiple test correction when testing each feature for association with an outcome. PCA is an unsupervised learning method and is similar to clustering<sup>1</sup>—it finds patterns without reference to prior knowledge about whether the samples come from different treatment groups or have phenotypic differences.

PCA reduces data by geometrically projecting them onto lower dimensions called principal components (PCs), with the goal of finding the best summary of the data using a limited number of PCs. The first PC is chosen to minimize the total distance between the data and their projection onto the PC (Fig. 1a). By minimizing this distance, we also maximize the variance of the projected points,  $\sigma^2$  (Fig. 1b). The second (and subsequent) PCs are selected similarly.



**Figure 2** | PCA reduction of nine expression profiles from six to two dimensions. (a) Expression profiles for nine genes (A–I) across six samples (a–f), coded by color on the basis of shape similarity, and the expression variance of each sample. (b) PC1–PC2 of the profiles in a. PC1 and PC2 reflect clearly visible trends, and the remaining capture only small fluctuations. (c) Transformed profiles, expressed as PC scores and  $\sigma^2$  of each component score. (d) The profiles reconstructed using PC1–PC3. (e) The 2D coordinates of each profile based on the scores of the first two PCs.

+  $y/\sqrt{2}$  (Fig. 1c). These coefficients are stored in a 'PCA loading matrix', which can be interpreted as a rotation matrix that rotates data such that the projection with greatest variance goes along the first axis. At first glance, PC1 closely resembles the linear regression line<sup>3</sup> of  $y$  versus  $x$  or  $x$  versus  $y$  (Fig. 1c). However, PCA differs from linear regression in that PCA minimizes the perpendicular distance

Lever et al., 2017 Nature Method 2017

# Additional information:



Why  $GH \leq 3$ ?

